

Values of government subsidies

MODE L	Decisions				Note
	e^*	r^*	l^*	p^*	
constra int	When $Cv < H(\alpha) \mid \alpha \in (\underline{\alpha}, \alpha_0), l = l'$				$H(\alpha) = \frac{(1+d)^4 (1-\alpha)^2 + (1+d)^2 + 8(1-\alpha) [2ak + \theta(1-\alpha)] + 16\theta^2 (1-\alpha)^2 - 192a^2 k^2 - 64}{256k(1-\alpha)^2}$ $\alpha = \frac{(1+d)^4 + 4a - 16k}{(1+d)^4 + 4a - 8k}, \alpha_0 = \frac{(1+d)^4 + 8(1+d)^2(\theta - 4) + 16(\theta - 10)\theta + 16k\sqrt{(1+d)^2 + 48\theta(4 - k)}}{(1+d)^4 + 8(1+d)^2(\theta - 2) + 16(\theta - 4)\theta - 192k^2}$
V(IG-I)	$\frac{8a\theta}{16(1-\alpha)} > 0$	$\frac{-\beta 8a\theta}{16(1-\alpha)} < 0$	$\frac{8a\theta}{16(1-\alpha)} > 0$	0	
V (BG-B)	$\frac{8a\theta}{16(1-\alpha)} > 0$	$\frac{-\beta 8a\theta}{16(1-\alpha)} < 0$	$\frac{8a\theta}{16(1-\alpha)} > 0$	0	The same to V(G-I)
	When $Cv > H(\alpha) \mid \alpha \in (\underline{\alpha}, \alpha_0), l = l'^A$				$l'^A = \frac{-2k\alpha + (-1+\alpha)\theta + 2\sqrt{k}\sqrt{cv(-1+\alpha)^2 + k\alpha^2 + \theta - \alpha\theta}}{(-1+\alpha)^2}$
Values (IG-I)	0	0	0	0	There is no improvement on optimal decisions when government provide subsidies in this situation.
V (BG-B)	0	0	0	0	There is no improvement on optimal decisions when government provide subsidies in this situation.

MODEL	VProfit				Note
	π_{SO}	π_{VM}	CS	SW	
constraint	When $Cv < H(\alpha) \mid \alpha \in (\underline{\alpha}, \alpha_0), l = l'$				$H(\alpha) = \frac{(1+d)^4 (1-\alpha)^2 + (1+d)^2 + 8(1-\alpha) [2ak + \theta(1-\alpha)] + 16\theta^2 (1-\alpha)^2 - 192a^2 k^2 - 64}{256k}$ $\alpha = \frac{(1+d)^4 + 4a - 16k}{(1+d)^4 + 4a - 8k}, \alpha_0 = \frac{(1+d)^4 + 8(1+d)^2(\theta - 4) + 16(\theta - 10)\theta + 16k\sqrt{(1+d)^2 + 48\theta(4 - k)}}{(1+d)^4 + 8(1+d)^2(\theta - 2) + 16(\theta - 4)\theta - 192k^2}$
Valu es (IG-I)	$\frac{\psi^2 - \theta^2}{128k(1-\alpha)^2} + \frac{g\alpha\theta}{(1-\alpha)} + gC_S$	$\frac{\psi^2 - \theta^2 + 32ak[\psi - \theta]}{256k(1-\alpha)^2}$	0	$\frac{3\psi^2 - 3\theta^2 + 256akg[ak + \theta(1-\alpha)]}{256k(1-\alpha)^2} + gC_S$	Always > 0
V (B G-B)	$\frac{\lambda^2 - \eta^2}{128k^{\beta}(1-\alpha)^2} + \frac{g\alpha\theta}{(1-\alpha)} + gC_S$	$\frac{\lambda^2 - \eta^2 + 32k^{\beta}a(\lambda - \eta)}{256k^{\beta}(1-\alpha)^2}$	0	$\frac{\lambda^2 - \eta^2 + 256k^{\beta}ga[\theta(1-\alpha) + k^{\beta}a]}{128k^{\beta}(1-\alpha)^2} + gC_S$	Always > 0
	When $Cv > H(\alpha) \mid \alpha \in (\underline{\alpha}, \alpha_0), l = l'^A$				$l'^A = \frac{-2k\alpha + (-1+\alpha)\theta + 2\sqrt{k}\sqrt{cv(-1+\alpha)^2 + k\alpha^2 + \theta - \alpha\theta}}{(-1+\alpha)^2}$
V(G-I)	$g\left[\frac{(w-ak)\alpha}{2(1-\alpha)^2} - \frac{a\theta}{(1-\alpha)} + C_S\right]$	0	0	$g\left[\frac{(w-ak)\alpha}{2(1-\alpha)^2} - \frac{a\theta}{(1-\alpha)} + C_S\right]$	When $C_S > \frac{a\theta}{(1-\alpha)} - \frac{(w-ak)\alpha}{2(1-\alpha)^2}$ SO is benefit
V(BG-B)	$g\left[\frac{(\mu-ak^{\beta})\alpha}{2(1-\alpha)^2} - \frac{a\theta}{(1-\alpha)} + C_S\right]$	0	0	$g\left[\frac{(\mu-ak^{\beta})\alpha}{2(1-\alpha)^2} - \frac{a\theta}{(1-\alpha)} + C_S\right]$	

Values of blockchain

MODE L	Decisions				Note
	e^*	r^*	l^*	p^*	
constra int	When $C_v < H(\alpha) \mid \alpha \in (\underline{\alpha}, \alpha_0), l = l^*$				$H(\alpha) = \frac{(1+d)^4 (1-\alpha)^2 + (1+d)^2 + 8(1-\alpha)[2\alpha k + \theta(1-\alpha)] + 16\theta^2(1-\alpha)^2 - 192\alpha^2 k^2 - 64}{256k(1-\alpha)^2}$ $\underline{\alpha} = \frac{(1+d)^2 + 4\theta - 16k}{(1+d)^2 + 4\theta - 8k}, \alpha_0 = \frac{(1+d)^2 + 8(1+d)^2(\theta-k) + 16\theta(1-\alpha) + 16k\sqrt{(1+d)^2 + 8\theta(\theta-4k)}}{(1+d)^2 + 8(1+d)^2(\theta-2k) + 16\theta(\theta-4k) - 192k^2}$
V (B-I)	$\frac{k\eta - k^B\theta}{16kk^B(1-\alpha)} > 0$	$\beta \frac{k^B\theta - k\eta}{16kk^B(1-\alpha)} < 0$	$\frac{k\eta - k^B\theta + \theta\theta(1-\alpha)(k^B - k)}{16kk^B(1-\alpha)} > 0$	$\frac{b}{2} > 0$	With the implementation of BEL, $e/l/p$ all increase. The premium rate decreases.
V (BG-IG)	$\frac{k\lambda - k^B\psi}{16kk^B(1-\alpha)} > 0$	$\beta \frac{k^B\psi - k\lambda}{16kk^B(1-\alpha)} < 0$	$\frac{k\lambda - k^B\psi + \theta\theta(1-\alpha)(k^B - k)}{16kk^B(1-\alpha)} > 0$	$\frac{b}{2} > 0$	The same as (VB-I)
When $C_v > H(\alpha) \mid \alpha \in (\underline{\alpha}, \alpha_0), l = l^A$					$l^A = \frac{-2k\alpha + (-1+\alpha)\theta + 2\sqrt{k}\sqrt{C_v(-1+\alpha)^2 + k\alpha^2 + \theta - \alpha\theta}}{(-1+\alpha)^2}$
V (B-I)	$\frac{k\mu - k^B w - \alpha k^B}{kk^B(1-\alpha)} > 0$	$\frac{\beta(k^B w - k\mu)}{kk^B(1-\alpha)} < 0$	$\frac{2(\mu - w) + 2\alpha(k - k^B)}{(1-\alpha)^2} > 0$	$\frac{b}{2} > 0$	
V (BG-IG)	$\frac{k\mu - k^B w - \alpha k^B}{kk^B(1-\alpha)} > 0$	$\frac{\beta(k^B w - k\mu)}{kk^B(1-\alpha)} < 0$	$\frac{2(\mu - w) + 2\alpha(k - k^B)}{(1-\alpha)^2} > 0$	$\frac{b}{2} > 0$	同 V (B-I)

M OD EL	VProfit				Note
	$V\pi_{SO}$	$V\pi_{VM}$	VCS	VSW	
co nst rai nt	When $C_v < H(\alpha) \mid \alpha \in (\underline{\alpha}, \alpha_0), l = l^*$				$H(\alpha) = \frac{(1+d)^4 (1-\alpha)^2 + (1+d)^2 + 8(1-\alpha)[2\alpha k + \theta(1-\alpha)] + 16\theta^2}{256k(1-\alpha)^2}$ $\underline{\alpha} = \frac{(1+d)^2 + 4\theta - 16k}{(1+d)^2 + 4\theta - 8k}, \alpha_0 = \frac{(1+d)^2 + 8(1+d)^2(\theta-k) + 16\theta(1-\alpha) + 16k\sqrt{(1+d)^2 + 8\theta(\theta-4k)}}{(1+d)^2 + 8(1+d)^2(\theta-2k) + 16\theta(\theta-4k) - 192k^2}$
V (B-I)	$\frac{k\eta^2 - k^B\theta^2}{128kk^B(1-\alpha)^2} - C_{SB},$ <p>when $C_{SB} < \frac{k\eta^2 - k^B\theta^2}{128kk^B(1-\alpha)^2}$, the SO is benefit. ($C_{SB} < \frac{\Delta k(1+d)^2 + k[b^2 + 2b(1+d)] + 48\Delta k}{32kk^B} - 2\Delta k$)</p>	$\frac{k\eta^2 - k^B\theta^2 + 32\alpha k k^B(\eta - \theta)}{256kk^B(1-\alpha)^2} - C_{VB}$ <p>, when $C_{VB} < \frac{k\eta^2 - k^B\theta^2 + 32\alpha k k^B(\eta - \theta)}{256kk^B(1-\alpha)^2}$, the VM is benefit.</p>	$\frac{b^2 + 2b(1+d)}{g} > 0$	$\frac{3k\eta^2 - 3k^B\theta^2 + 32\alpha k k^B(\eta - \theta)}{256kk^B(1-\alpha)^2} + \frac{b^2 + 2b(1+d)}{g} - C_{SB} - C_{VB}$ <p>When $C_{SB} + C_{VB} < \frac{3k\eta^2 - 3k^B\theta^2 + 32\alpha k k^B(\eta - \theta)}{256kk^B(1-\alpha)^2} + \frac{b^2 + 2b(1+d)}{g}$</p>	
V (BG-IG)	$\frac{k\lambda^2 - k^B\psi^2}{128kk^B(1-\alpha)^2} - C_{SB},$ <p>when $C_{SB} < \frac{k\lambda^2 - k^B\psi^2}{128kk^B(1-\alpha)^2}$, the SO is benefit.</p>	$\frac{k\lambda^2 - k^B\psi^2 + 32\alpha k k^B(\lambda - \psi)}{256kk^B(1-\alpha)^2} - C_{VB}$ <p>, when $C_{VB} < \frac{k\lambda^2 - k^B\psi^2 + 32\alpha k k^B(\lambda - \psi)}{256kk^B(1-\alpha)^2}$, the VM is benefit.</p>	$\frac{b^2 + 2b(1+d)}{g} > 0$	$\frac{3k\lambda^2 - 3k^B\psi^2 + 32\alpha k k^B(\lambda - \psi)}{256kk^B(1-\alpha)^2} + \frac{b^2 + 2b(1+d)}{g} - C_{SB} - C_{VB}$	Similar to V(B-I)
When $C_v > H(\alpha) \mid \alpha \in (\underline{\alpha}, \alpha_0), l = l^A$					

$V(B-I)$	$\frac{k(\mu - \alpha k^2)[\gamma - \delta(\mu - \alpha k^2)] - k^2(w - \alpha k)[\theta - \delta(w - \alpha k)]}{4kk^2(1 - \alpha)^2} - C_{SB}$	<p><i>0, no matter what the cost of blockchain, there is no effect on VM when he implement the technology.</i></p>	$\frac{b^2 + 2b(1 + d)}{8} > 0$	$\frac{k(\mu - \alpha k^2)[\gamma - \delta(\mu - \alpha k^2)] - k^2(w - \alpha k)[\theta - \delta(w - \alpha k)]}{4kk^2(1 - \alpha)^2} - C_{SB} + \frac{b^2 + 2b(1 + d)}{8}$	
$V(B-G-I-G)$	$\frac{k(\mu - \alpha k^2)[\lambda - \delta(\mu - \alpha k^2)] - k^2(w - \alpha k)[\psi - \delta(w - \alpha k)]}{4kk^2(1 - \alpha)^2} - C_{SB}$	<p>0</p>	$\frac{b^2 + 2b(1 + d)}{8} > 0$	$\frac{k(\mu - \alpha k^2)[\lambda - \delta(\mu - \alpha k^2)] - k^2(w - \alpha k)[\psi - \delta(w - \alpha k)]}{4kk^2(1 - \alpha)^2} - C_{SB} + \frac{b^2 + 2b(1 + d)}{8}$	<p><i>Similar to V(B-I)</i></p>